# Single-Stage Boost Inverter With Coupled Inductor

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Abstract—Renewable power systems as distributed generation units often experience big changes in the inverter input voltage due to fluctuations of energy resources. Often, a front-end boost converter is added to step up the dc voltage when the energy resources are at a weak point. However, when a very high boost gain is demanded, the duty cycle may come to its extreme, and large duty cycles causes serious reverse-recovery problems. This paper proposes a novel single-stage boost-type inverter with coupled inductor. By introducing impedance network, including coupled inductor, into the three-phase bridge inverter, and adjusting the previously forbidden shoot-through zero state, the converter can realize a high boost gain and output a stable ac voltage. The single-stage operation of the converter may lead to improved reliability and higher efficiency. Theoretical analysis, simulation, and experimental results are presented to verify good performance.

*Index Terms*—Boost inverter, coupled inductor, shoot-through zero state, single stage.

#### I. INTRODUCTION

■ HE increasing tension on the global energy supply has resulted in greater interest in renewable energy resources [1]. This presents a significant opportunity for distributed power generation (DG) systems using renewable energy resources, including wind turbines, photovoltaic (PV) generators, small hydro systems, and fuel cells [2]-[4]. However, these DG units produce a wide range of voltages due to the fluctuation of energy resources and impose stringent requirements for the inverter topologies and controls [5]. Usually, a boost-type dc-dc converter is added in the DG units to step up the dc voltage [6]–[8]. This kind of topology, although simple may not be able to provide enough dc voltage gain when the input is very low, even with an extreme duty cycle. Also, large duty cycle operation may result in serious reverse-recovery problems and increase the ratings of switching devices. Furthermore, the added converter may deteriorate system efficiency and increase system size, weight, and cost. On the other hand, the upper and lower devices of the same phase leg cannot be gated on simultaneously in conventional voltage source inverter (VSI). Otherwise, shoot-through problems would occur and destroy the switching devices. Dead time is always used in case of shoot-through events in bridge type converters, but it will cause waveform distortion. Though dead-time compensation technology [9], [10]

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Digital Object Identifier 10.1109/TPEL.2011.2165855

has been developed, it increases control complexity. So, it is desirable to have a single-stage high-gain boost inverter featuring no shoot through issues.

Single-stage topologies, which integrate performance of each stage in a multistage power converter, are becoming the focus of research. Though they may cause increased control complexity, they may offer higher efficiency, reliability, and lower cost. It is observed that many single-stage voltage source [11]-[13] and current source [14], [15] inverters have been proposed. A Z-source inverter (ZSI) proposed in [16] is able to overcome the problems in conventional VSI and conventional current source inverter. It can provide a wide range of obtainable voltage and has been applied to renewable power generation systems [17]-[19]. However, this topology is complex and inductors and capacitors in the Z-network should have high consistency. Moreover, only shoot-through zero state can be regulated when higher voltage gain is required. Widening shoot-through zero state will decrease modulation index and output voltage amplitude. Also, in order to completely avoid the unwanted operation modes, the input diode should be replaced by a switch which turns ON during all active states and traditional zero states [20]. Four quasi-Z-source inverters (qZSIs) derived from the conventional ZSI have been proposed in [21], whose basic principles are similar to those of conventional ZSI. Corresponding control methods and application conditions of conventional ZSI also fit for the qZSIs in theory. Anderson and Peng [21] show some advantages of qZSIs over conventional ZSI, such as lower voltage/current stress of impedance network and lower switch voltage stress. Nevertheless, they do not overcome the limits of conventional ZSI described earlier.

This paper presents a novel single-stage boost inverter with a unique impedance network including coupled inductor. The bus voltage can be stepped up by using shoot-through zero state to store and transfer energy within the impedance network. Just as with ZSI, the single-stage boost inverter completely avoids destroying devices during shoot-through zero states. So, it has improved reliability. Second, the inductors and capacitors do not have to be of high consistency, leading to easier circuit parameters design. Third, both shoot-through zero states and coupled inductor's turn ratio can be regulated to control the boost gain. So, the output voltage can be regulated in a wide range and can be stepped up to a higher value. Finally, the bus voltage equals the sum of the capacitor voltages, and it is higher than each capacitor voltage. This ensures status capacitor voltage ratings can be fully utilized. The single-stage boost inverter with coupled inductor is suitable for applications where the input voltage varies from a relative low level to a higher level continuously while outputting a stable ac voltage. Operating principles of the novel inverter are presented in Section II. Section III analyzes the equivalent circuit, boost feature under two different modes, and its control strategy. In Section IV, the coupled inductor is

Manuscript received February 28, 2011; revised May 11, 2011 and June 27, 2011; accepted August 12, 2011. Date of current version February 20, 2012. Recommended for publication by Associate Editor M. Vitelli.



Fig. 1. Topology of single-stage boost inverter with coupled inductor.



Fig. 2. Relationship between the generator output power and rotational speed.

analyzed. Finally, simulation and experiment results are included in Section V.

#### II. PROPOSED SINGLE-STAGE BOOST INVERTER

Fig. 1 shows the general structure of the proposed singlestage boost inverter. It employs a unique impedance network to combine the three-phase inverter bridge with the power source. The impedance network does not introduce any switching devices and may lead to improved reliability, higher efficiency, and lower cost. To extend the operation range of the inverter, coupled inductor with a low leakage inductance is used. The dc source can be a battery, diode rectifier, fuel cell, or PV cell. To describe the operating principle and characteristics, this paper focuses on one application example of the single-stage boost inverter: a single-stage boost inverter for wind power generation.

For wind power generation system, variable speed wind turbine is often adopted because it is known to provide more effective power tracking than fixed speed wind turbines [22]. Fig. 2 presents the relationship between the generator power output and rotational speed relating to wind speed changes. Note that the output power of wind turbine may be at a low level under a weak wind condition. Fig. 3 shows the conventional twostage power conversion for wind power generation. A front-end dc-dc boost converter is added to step up bus voltage especially under weak wind condition, because the conventional VSI cannot produce an ac voltage larger than the dc input voltage. The proposed single-stage boost inverter for wind power generation application is shown in Fig. 4. The system can produce an ac voltage larger or smaller than the input dc voltage with single stage operation. The diode  $D_1$  in series with  $L_p$  is necessary for preventing reverse current flow.



Fig. 3. Traditional two-stage power conversion for wind power generation.



Fig. 4. Single-stage boost inverter with coupled inductor for wind power generation.

# III. OPERATION PRINCIPLE, BOOST FEATURE ANALYSIS, AND CONTROL STRATEGY

Conventional VSI has eight possible switching states [23], of which two are zero states and six are active states. Two zero states make load terminals shorted through, and can be assumed by turning on upper or lower three devices, respectively. Six active states can be assumed by turning on the switches from different phase legs, when the input dc voltage is applied across the load. However, the three-phase single-stage boost inverter has one extra zero state when the load terminals are shorted through both the upper and lower devices of any one phase leg, any two phase legs, or all three phase legs. To distinguish the two kinds of zero state mentioned earlier, we call the two zero states open-zero states, and the extra zero states shootthrough zero state. Shoot-through zero state is forbidden in the conventional VSI because it would make device failure events happen. Combined with the impedance network in front of the three-phase bridge, the shoot-through zero state provides the unique boost feature to the inverter. It should be noted that shoot-through zero states are allocated into open-zero states without changing the total open-zero state time intervals. That is, the active states are unchanged. Thus, the shoot-through zero state does not affect the pulsewidth modulation (PWM) control of the inverter, because it equivalently produces the same zero voltage as the open-zero state to the load terminal.

Fig. 5 shows equivalent circuits of the single-stage boost inverter under three switching states.

State 1: The converter is in shoot-through zero state under this duration, as shown in Fig. 5(a). Bus voltage  $v_b$  was shorted to ground and diode  $D_2$  is reversely biased. Input dc voltage is applied across primary winding of the coupled inductor, making primary current linearly increase. The inductive voltage of secondary winding charges  $C_1$ . At the same time,  $C_2$  is discharged by  $L_1$  with linearly increasing current, assuming that the capacitor voltage is constant.

*State 2*: During this interval, the converter is in one of the two traditional open-zero states, as shown in Fig. 5(b). Inductor  $L_1$ 



Fig. 5. Equivalent circuit under three switching states. (a) Shoot-through zero state. (b) Open-zero state. (c) Active state.

and secondary winding of the coupled inductor charge capacitors  $C_1$  and  $C_2$  through diode  $D_2$ , respectively. In this state, the current of inductor  $L_1$  decreases from peak value to zero.

State 3: When the circuit is in one of the six active states, as shown in Fig. 5(c), diode  $D_3$  is reverse biased. The energy stored in the coupled inductor and  $C_1$  releases to the load, and the bus voltage is stepped up to a higher level.

Two boost modes can be achieved by regulating the shootthrough zero state as well as configuring the turn ratio and coupling coefficient of the coupled inductor. Operating principle of the single-stage boost inverter is analyzed under these two modes. When applying the converter to voltage drop compensation or applications where lower boost gain is needed, the inductance of coupled inductor should be designed large enough to ensure its continuous current-mode operation. When higher boost gain is required, the inductance of the primary winding  $L_p$  should be as small as to keep the circuit working in discontinuous current mode. Fig. 6 shows coupled inductor current waveform in one shoot-through period  $T_{\rm sh}$  under two operation



Fig. 6. Coupled inductor current waveforms under two operation modes. (a) Inductor  $L_p$  works in CCM. (b) Inductor  $L_p$  works in DCM.

modes, respectively. Note that the shoot-through period  $T_{\rm sh}$  is the equivalent switching period viewed from the impedance network, which is not equivalent to the switching period  $T_s$  of the inverter bridge.  $T_{\rm sh}$  may be two or six times of  $T_s$ , determined by the modulation scheme it used [16], [24], [25], which reduces the required size and weight of the coupled inductor.

### A. Lower Voltage Boost Gain Mode

In lower voltage boost gain applications, the key characteristic is that the current through  $L_p$  generally works in continuous mode, as shown in Fig. 6(a).

Define the shoot-through duty cycle  $D_0$  as the time when the three-phase bridge is in shoot-through state, and the duty cycle  $1 - D_0$  as the time when the three-phase bridge is in nonshoot-through state, the average voltage across the primary winding during one shoot-through period can be expressed as

$$\langle v_{Lp}(t) \rangle_{T_{\rm sh}}^{\rm CCM} = D_0 V_i + (1 - D_0) (V_i - v_b) = 0.$$
 (1)

From (1), the amplitude of bus voltage can be expressed as follows:

$$\hat{v}_b = \frac{1}{1 - D_0} \times V_i. \tag{2}$$

Define *B* as the boost gain,  $B = \hat{v}_b V_i$ , which can be expressed as

$$B = \frac{1}{1 - D_0}.$$
 (3)

The boost gain is similar to that of conventional dc–dc boost converter in this boost mode.

#### B. Higher Voltage Boost Gain Mode

In higher voltage boost gain applications, the key characteristic is that the inductance of primary winding is less than that of secondary winding, and primary winding current generally works in discontinuous mode, as shown in Fig. 6(b).

Define the coupling coefficient as

$$k = \frac{M}{\sqrt{L_p \times L_s}} \tag{4}$$

where  $L_p$ ,  $L_s$ , and M are the self-inductance of each winding and the mutual inductance, and the effective turn ratio

$$N_e = \sqrt{\frac{L_s}{L_p}}.$$
(5)

Define the duty cycle  $D_1$  as the time when the inductor  $L_p$  current decreasing from peak value to zero, the average voltage across the both sides of coupled inductor during one shoot-through period can be expressed as

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$$\langle v_{L_p}(t) \rangle_{T_{\rm sh}}^{\rm DCM} = D_0 V_i + D_1 (V_i - v_b)$$
  
  $+ (1 - D_0 - D_1) \frac{k (V_{c1} - v_b)}{N_e} = 0$  (6)

$$\langle v_{L_s}(t) \rangle_{T_{\rm sh}}^{\rm DCM} = D_0 V_{c1} + (1 - D_0) (V_{c1} - v_b) = 0.$$
 (7)

From (6) and (7), the amplitude of bus voltage can be expressed as

$$\hat{v}_b = \frac{(D_0 + D_1) N_e}{D_1 N_e + D_0 (1 - D_0 - D_1) \times k} \times V_i.$$
(8)

Define physical turn ratio of ideal transformer as  $N = N_s/N_p$ . According to the relationship of  $N_e$  and N:  $N_e = N \times k$ , (8) can be simplified as

$$B = \frac{\hat{v}_b}{V_i} = \frac{(D_0 + D_1)N}{D_1 N + D_0(1 - D_0 - D_1)}.$$
 (9)

The output peak phase voltage  $\hat{v}_{ac}$  generated by the inverter can be expressed as

$$\hat{\nu}_{\rm ac} = m B \frac{V_i}{2} \tag{10}$$

where *m* is the modulation index,  $m \le 1$  for synchronized PWM (SPWM), and  $m \le 2/\sqrt{3}$  for space vector PWM. The output ac voltage can be stepped up or down by choosing an appropriate voltage gain *G* 

$$G = m \times B. \tag{11}$$

From (11), the voltage gain G is determined by the modulation index m and boost gain B. The available output ac voltage is able to change in a wide range by regulating G. The boost gain B as expressed in (9) can be controlled by shoot-through duty cycle  $D_0$ , duty cycle  $D_1$ , and physical turn ratio N of the coupled inductor. It should be noted that the available shoot-through duty cycle is limited by the traditional open-zero duty cycle which is determined by the modulation index m. The shoot-through zero state does not affect the PWM control of the inverter, because it equivalently produces the same voltage to the load terminal. As analyzed earlier, by designing different coupled inductor and regulating the duty cycle, the single-stage boost inverter not only can be applied to voltage drop compensation or applications where lower boost gain is needed, but it can also can be applied to higher boost requirements.

The capacitor  $C_1$  and  $C_2$  voltage are dependent on the shootthrough state and can be stepped up by changing the shootthrough duty cycle. The average bus voltage is identical to the capacitor  $C_1$  voltage because the average voltage across secondary winding of coupled inductor during one shoot-through



Fig. 7. Relation curve of duty cycle  $D_0$ ,  $D_1$ , and input voltage  $V_i$ .

period is zero. The capacitor  $C_1$  and  $C_2$  voltage can be expressed as

$$V_{c1} = \hat{v}_b \times (1 - D_0) \tag{12}$$

$$V_{c2} = \hat{v}_b \times D_0. \tag{13}$$

When the voltage at the diode bridge output provided by the generator in wind power generation system is approximately 300  $V_{dc}$ , without any boost mode, the voltage at the inverter bridge input will also be approximately 300  $V_{dc}$ . The inverter can only output a phase voltage of 106  $V_{rms}$  based on SPWM control under modulation index *m* being 1. In order to obtain phase voltage of 220  $V_{rms}$ , the minimum voltage at the inverter bridge input must be greater than 620  $V_{dc}$ . Therefore, the voltage at the diode bridge output needs to be boosted, and the single-stage boost inverter with higher boost gain should be used.

According to aforementioned analysis, in higher voltage boost gain applications, boost gain *B* as expressed in (9) is not only determined by shoot-through duty cycle  $D_0$ , but also by duty cycle  $D_1$ , and the physical turn ratio of coupled inductor. Duty cycle  $D_1$  can be expressed as

$$D_1 = \frac{[NV_i - (1 - D_0)\,\hat{v}_b]\,D_0}{(N - D_0)\,\hat{v}_b - NV_i}.$$
(14)

From (14), we know that when physical turn ratio N is determined, duty cycle  $D_1$  varies with shoot-through duty cycle  $D_0$ , input voltage  $V_i$ , and bus voltage  $v_b$ . Bus voltage amplitude of the converter is regulated by closed-loop control of shoot-through duty cycle, so  $D_1$  only varies with input voltage  $V_i$  when bus voltage amplitude is preset. Fig. 7 graphically illustrates the relationship between shoot-through duty cycle  $D_0$ , duty cycle  $D_1$ , and input voltage  $V_i$ , given a constant physical turn ratio. From Fig. 7, we know that when shoot-through duty cycle  $D_0$  is determined, duty cycle  $D_1$  have a certain relationship with input voltage  $V_i$ .

According to  $N_e = N \times k$ , (14) can be rewritten as

$$D_1 = \frac{[N_e/k - (1 - D_0) B] D_0}{(N_e/k - D_0) B - N_e/k}.$$
(15)

Combined with (5) and (15), we know that when inductances of the coupled inductor are fixed, the effective turn ratio  $N_e$ is determined. Because bus voltage is regulated by means of closed-loop control of shoot-through zero state, duty cycle  $D_1$ 



Fig. 8. Boost gain B versus shoot-through duty cycle  $D_0$ .

only varies with coupling coefficient k when boost gain is determined. Fig. 8 graphically illustrates the boost gain B versus shoot-through duty cycle  $D_0$ , when inductances of the coupled inductor are fixed. In Fig 8 (a), mode 1,  $D_1 = 0$ , primary winding current decreases from peak value to zero instantly when the coupled inductor is under unity coupling condition. The boost gain of mode 1 is theoretically the maximum gain that the singlestage boost inverter can obtain with a given shoot-through zero state:  $N/1 - D_0$ . While in Fig. 8 (b), mode 2,  $D_1 = 1 - D_0$ , primary winding works in continuous current mode. The boost gain is potentially at its minimum value that the single-stage boost inverter can obtain with a given shoot-through zero state:  $1/1 - D_0$ .

The previous analysis reveals that 1) with a determined physical turn ratio N of the coupled inductor, only shoot-through zero state is required to be regulated to step up and stabilize the bus voltage when input voltage varies in a wide range; and 2) given a constant shoot-through duty cycle  $D_0$ , duty cycle  $D_1$ decreases and boost gain B increases as coupling coefficient kincreases. In other words, when boost gain is determined, duty cycle  $D_0$  can be decreased to a certain degree by increasing the coupling coefficient k, which brings the benefit of reducing primary winding current ripple.

All the traditional PWM schemes can be used to control the inverter. Fig. 9 shows the maximum constant boost control method with third-harmonic injection [25]. The equivalent dcbus voltage is boosted because of the shoot-through zero states. Shooting through three phase legs at the same time can reduce the current stress of each device, while the switching frequency is doubled. Meanwhile, the shoot-through states should preferably have the same time duration to minimize the size of the impedance network. When the modulation index *m* is set, the shoot-through duty cycle  $D_0$  versus modulation index *m* can be expressed as follows:

$$D_0 = 1 - \frac{\sqrt{3}m}{2}.$$
 (16)

So, the maximum shoot-through duty cycle is limited by modulation index. When the modulation index is set to no less than 0.8, the shoot-through duty cycle is limited to 0.307. The dashed area of Fig. 8 is the possible operation area of the inverter when N = 2.5.



Fig. 9. Maximum constant boost control method with third-harmonic injection.

#### IV. COUPLED INDUCTOR DESIGN ANALYSIS

As analyzed earlier, the bus voltage of the proposed converter can be stepped up to a higher level by regulating the shoot-through duty cycle and configuring the turn ratio and the coupling coefficient of the coupled inductor. This paper takes higher voltage boost gain applications as an example to demonstrate the operating principle of coupled inductor in detail.

# A. Transformer Model of Coupled Inductor

Transformer model can be derived mathematically [26] and can be expressed by the following equations:

$$v_p = L_p \frac{di_p}{dt} + M \frac{di_s}{dt}$$
$$v_s = M \frac{di_p}{dt} + L_s \frac{di_s}{dt}$$
(17)

where mutual inductance M is positive under direct coupling condition. The expressions can be rearranged as follows:

$$v_p = L_p \left( 1 - \frac{M^2}{L_p L_s} \right) \frac{di_p}{dt} + \frac{M}{L_s} v_s$$
$$v_s = \frac{M}{L_p} v_p + L_s \left( 1 - \frac{M^2}{L_p L_s} \right) \frac{di_s}{dt}.$$
(18)

Assuming that  $L_p = L$ , (4) and (5) can be expressed as

$$L_s = N_e^2 L_p = N^2 k^2 L$$
  

$$M = k \sqrt{L_p L_s} = k^2 N L.$$
(19)

According to (4) and (19), (18) can be simplified as

$$v_{p} = L \left(1 - k^{2}\right) \frac{di_{p}}{dt} + \frac{1}{N} v_{s}$$
$$v_{s} = k^{2} N v_{p} + (Nk)^{2} \left(1 - k^{2}\right) L \frac{di_{s}}{dt}.$$
 (20)

According to (20), an equivalent circuit can be constructed as shown in Fig. 10, where  $(1 - k^2)L$  and  $k^2 L$  refer to leakage inductance  $L_k$  and magnetizing inductance  $L_m$ , respectively. This circuit is one form of the transformer models for coupled



Fig. 10. Equivalent circuit of coupled inductor.

inductor, where the leakage inductor appears only on one side. Hence, the coupled inductor is modeled as a magnetizing inductor, an ideal transformer with a turn ratio of N, and a leakage inductor.

#### B. Coupled Inductor Design Guideline

Rewrite (17) as

$$v_p - \frac{k}{N_e} v_s = \left(1 - k^2\right) L \frac{di_p}{dt}$$
$$v_s - N_e k v_p = N_e^2 \left(1 - k^2\right) L \frac{di_s}{dt}.$$
 (21)

If the relationship of  $v_p$  and  $v_s$  can be found in different time intervals during one shoot-through period  $T_{\rm sh}$ , (21) can be expressed as

$$v_{p} = L_{eq_{-p}} \frac{di_{p}}{dt}$$

$$v_{s} = L_{eq_{-s}} \frac{di_{s}}{dt}$$
(22)

where  $L_{eq_p}$  and  $L_{eq_s}$  are equivalent inductances of the coupled inductor at different time intervals. It is the same format as the noncoupling inductor. The relationship of  $v_p$  and  $v_s$  changes at different time intervals during one shoot-through period. Thus, during different time intervals, the equivalent inductances in (22) are different. As analyzed in Section III, in higher voltage boost gain applications, one shoot-through period  $T_{sh}$  can be divided into three parts:  $T_0 = D_0 T_{sh}$ ,  $T_1 = D_1 T_{sh}$ , and  $T_2 = (1 - D_0 - D_1)T_{sh}$ . According to the transformer model constructed earlier, the equivalent inductances can be expressed as

$$L_{eq0\_p} = \frac{1-k^2}{1-((1-D_0)(D_0+D_1)/D_1N+D_0(1-D_0-D_1)))}L$$

$$T_0:$$

$$L_{eq0\_s} = \frac{N^2 k^2 \left(1 - k^2\right)}{1 - \left(\left[D_1 N - D_0 \left(D_0 + D_1 - 1\right)\right] k^2 / \left(1 - D_0\right) \left(D_0 + D_1\right)\right)}L$$
(23)

$$L_{\text{eq1\_}p} = \frac{1 - k^2}{1 - (D_0 + D_1/N - (1 - D_0 - D_1))}L$$
  
T<sub>1</sub>:

$$L_{\text{eq1\_s}} = \frac{N^2 k^2 \left(1 - k^2\right)}{1 - \left(\left[N - \left(1 - D_0 - D_1\right)\right] k^2 / D_0 + D_1\right)} L$$
(24)



Fig. 11.  $L_{eqx_p}/L \text{ or } L_{eqx_s}/L \text{ versus duty cycle } D_0 \text{ and } D_1, (x = 0, 1, 2). (a)$  $L_{eq0_p}/L. (b) L_{eq0_s}/L. (c) L_{eq1_p}/L. (d) L_{eq1_s}/L. (e) L_{eq2_p}/L. (f) L_{eq2_s}/L.$ 

$$L_{eq2\_p} = 0$$

$$T_2:$$

$$L_{eq2\_s} = N^2 k^2 L.$$
(25)

In higher voltage boost gain applications, primary winding generally works in discontinuous current mode. So, in the active states,  $L_{eq2_p}$  is equal to zero because primary winding current is zero.

After the bus voltage amplitude and parameters of the coupled inductor are confirmed, the equivalent inductance of different time intervals varies with duty cycle  $D_0$  and  $D_1$ . Fig. 11 graphically illustrates  $L_{eqx_p}/L$  or  $L_{eqx_s}/L$  versus duty cycle  $D_0$  and  $D_1$ , (x = 0, 1, 2) when N = 2.5 and k = 0.95. In  $T_0$  and  $T_1$  of one shoot-through period  $T_{sh}$ , secondary equivalent inductance versus  $L: L_{eq0_s}/L$  and  $L_{eq1_s}/L$ , are negative because secondary winding current is opposite to the reference direction shown in Fig. 1.

Taking the input/output parameters of experimental prototype as an example, according to the equivalent inductance expressions at different time intervals of one shoot-through period  $T_{\rm sh}$ and the relationship of inductor voltage and current, which can



Fig. 12. Waveform of primary winding current.



Fig. 13. Simulation and prototype system configuration.



Fig. 14. Control circuit diagram for inverter switches.

be expressed as

$$i_{p(n)} = i_{p(n-1)} + \frac{v_p}{L_{\text{eqx},p}}t, \qquad \begin{cases} n = 1, \ 2, \ 3\\ x = 0, \ 1, \ 2 \end{cases}$$
 (26)

then the primary winding current waveform can be obtained, as shown in Fig. 12. From (26), we know that the primary equivalent inductance determines the current ripple of primary winding. If limiting the current amplitude to  $I_m$ , the primary equivalent inductance during the shoot-through zero state can be expressed as

$$L_{\rm eq0\_p} = \frac{V_i \times D_o \times T_{\rm sh}}{I_m}.$$
 (27)

According to (23), the primary winding inductance  $L_p$  can be obtained from the relationship of primary equivalent inductance and actual primary winding inductance in one shoot-through zero state. The secondary winding inductance can also be found according to (5).







Fig. 15. Simulation waveforms.

#### V. SIMULATION AND EXPERIMENTAL RESULTS

Simulation has been performed to confirm the previous analysis. Fig. 13 shows the circuit configuration with the circuit parameters as:  $V_i = 300$  V,  $L_p = 332.3 \mu$ H,  $L_s = 1.87$  mH, k = 0.95,  $C_1 = 10 \mu$ F,  $C_2 = 40 \mu$ F,  $L_1 = 30 \mu$ H, and Po = 800 VA. The system is intended to produce a three-phase



Fig. 16. Experimental waveforms. (a) Input dc voltage  $V_i$  and bus voltage  $v_b$ . (b) Primary winding current  $i_p$  and bus voltage  $v_b$ . (c) Input dc voltage  $V_i$  and output phase voltage  $v_a b$ . (d) Input dc voltage  $V_i$  and output phase voltage  $v_a b$  when input voltage changes from 350 to 250 V.

220 V ac output from a relative low level input source. Fig. 14 shows the control circuit diagram for inverter switches. Fig. 15 shows the simulation waveforms. It is clear that the bus voltage is stepped up to 700 V, indicating a successful boost inverting operation of the converter. In this case, the modulation index was set to 0.86, the shoot-through duty cycle was set to 0.255, and the switching frequency was 8 kHz. The shoot-through zero state was inserted in every traditional open-zero state, achieving an equivalent switching frequency of 16 kHz viewed from the impedance network. Fig. 15(c) illustrates that the output phase voltage is constant during input voltage transient.

A prototype, as shown in Fig. 13, has been constructed. The same parameters as the simulation were used. Fig. 16 shows the experimental results. When the input voltage is low, as shown in Fig. 16(a) and (c), the shoot-through zero state was regulated to boost the amplitude of bus voltage to about 700 V, enough to output the desired ac voltage. The total harmonic distortion of output voltage is 1.71%. Fig. 16(d) shows a constant output phase voltage when input voltage varies from 350 to 250 V. The waveforms are consistent with the simulation results. By controlling the shoot-through duty cycle  $D_0$  or the boost gain B when the coupled inductor has been designed, the desired output voltage can be obtained even when the input voltage is at a low level. The tested efficiency only achieves 83.4%. This may be because the circuit parameters have not been optimized.

### VI. CONCLUSION

This paper has presented a novel single-stage boost inverter with coupled inductor, which exhibits several merits.

- It employs a unique impedance network including coupled inductor to connect the three-phase inverter bridge to the power source. By designing the coupled inductor properly and adjusting the previously forbidden shoot-through zero state, the magnitude of the bus voltage can be greatly stepped up.
- By configuring turn ratio and coupling coefficient of the coupled inductor differently, the impedance network can work in two boost modes making it suitable for different inverting applications.
- 3) Shoot-through states, which are forbidden in conventional VSIs, are utilized to store and transfer energy within the impedance network to boost the amplitude of the bus voltage. Waveform distortion of the ac output voltage caused by dead time is essentially avoided.

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